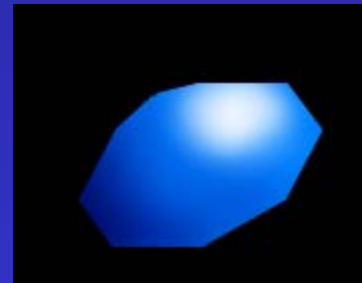
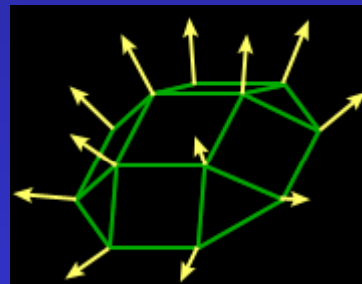
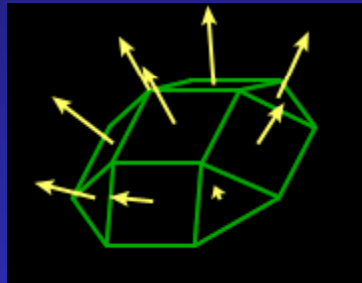


# Smooth Shading

## Gouraud

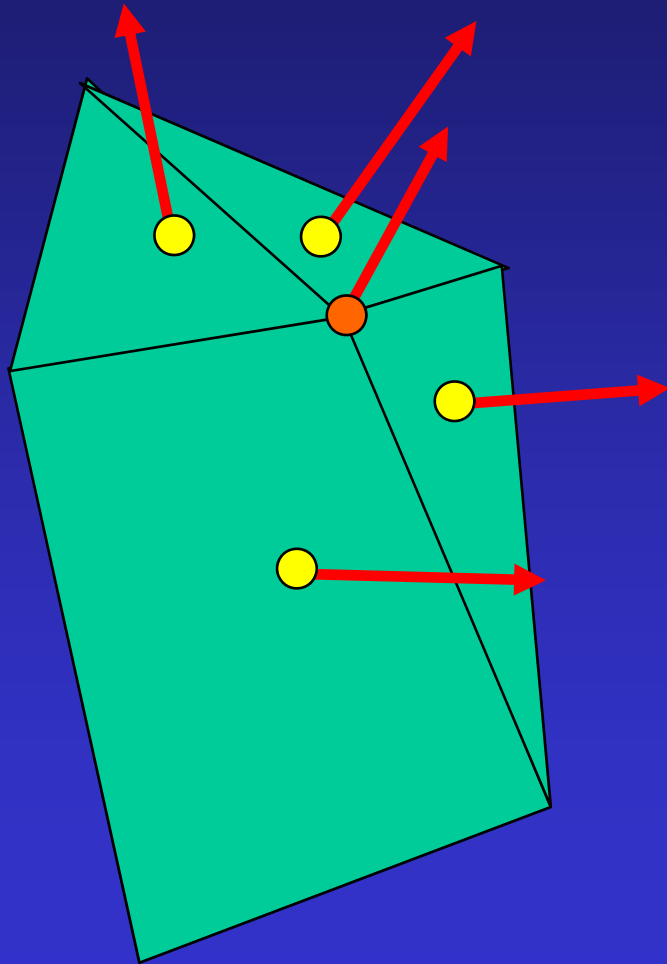
## Phong

# Interpolate value(s) for point in face from values at vertices



<http://www.blancmange.info/notes/maths/vectors/primitives/>

# Interpolate normals at vertices



For each vertex,  $v$

$$N_v = \langle 0, 0, 0 \rangle$$

For each face of vertex

Compute face normal

$$N_v += \text{face normal}$$

Normalize  $N_v$

For each vertex,  $v$

$$N_v = \langle 0, 0, 0 \rangle$$

For each face

Compute face normal

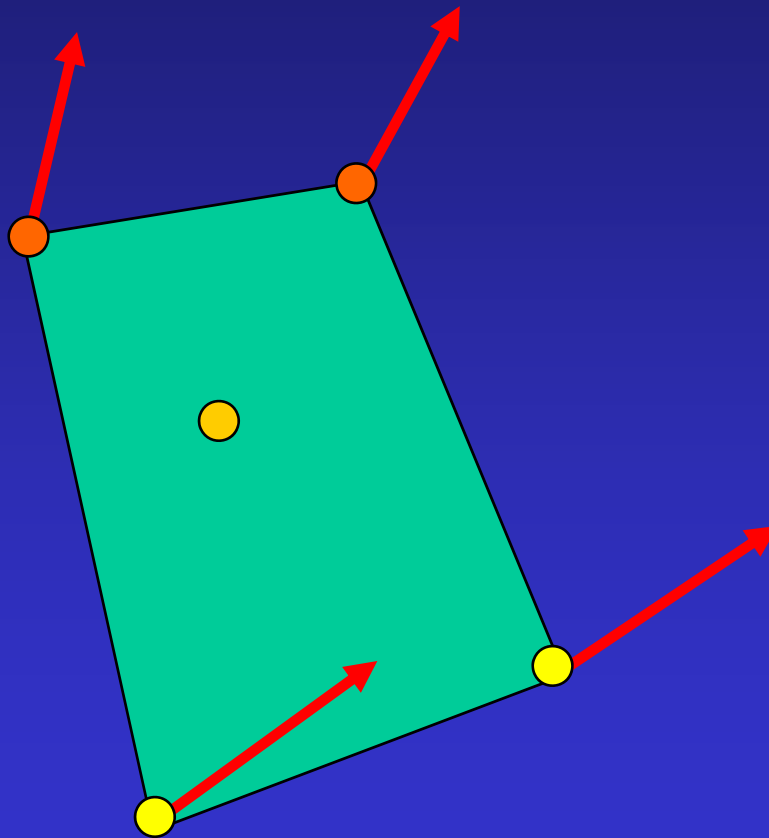
For each vertex of face

$$N_v += \text{face normal}$$

For each vertex,  $v$

Normalize  $N_v$

# Interpolate value(s) for point in face from values at vertices



## Gouraud smooth shading:

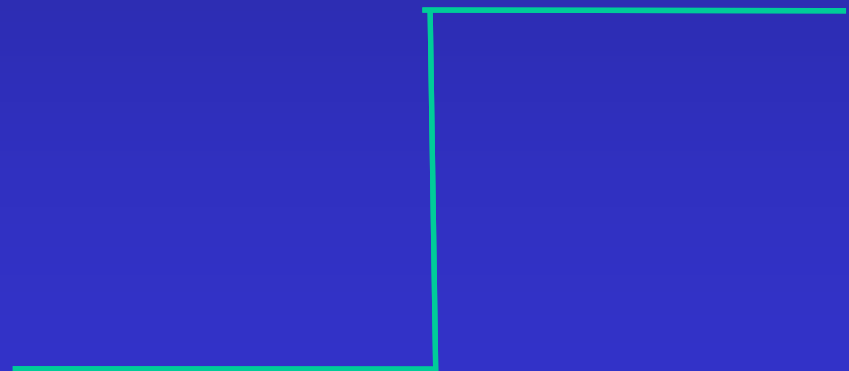
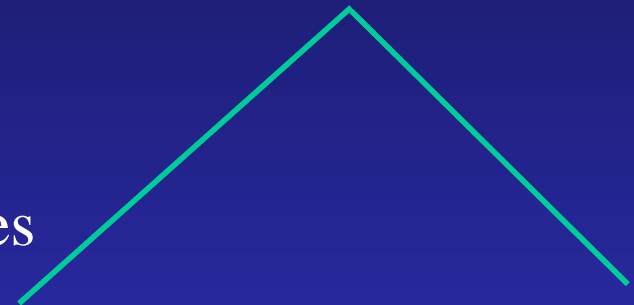
- Compute normals at vertices
- Compute color at vertices
- Interpolate interior color

# Mach Band Effect

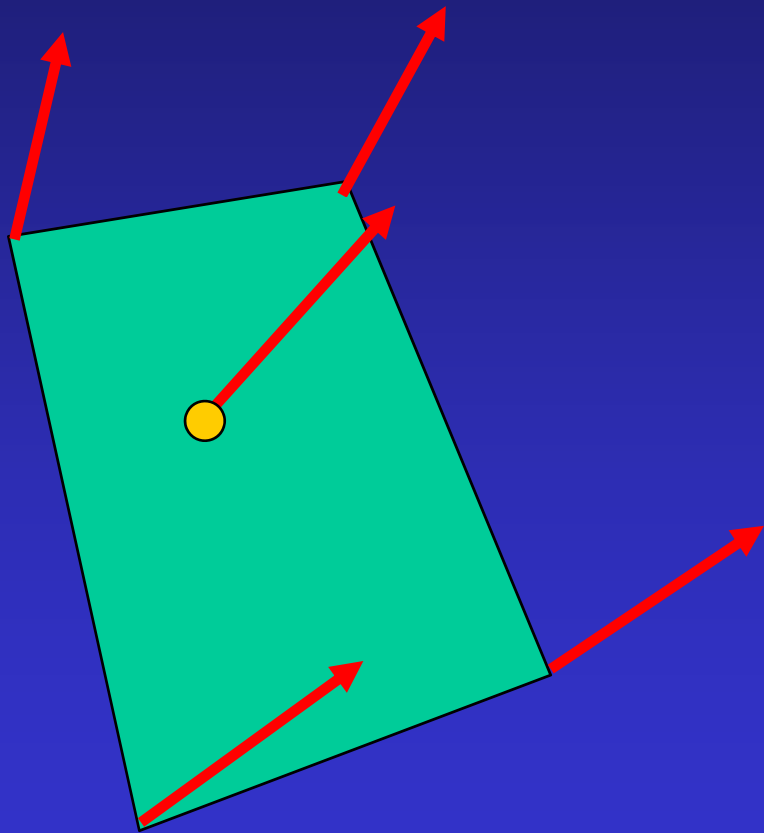
Smoothly shaded objects

Colors are continuous, but not derivatives

Eye picks up on this and accentuates discontinuity



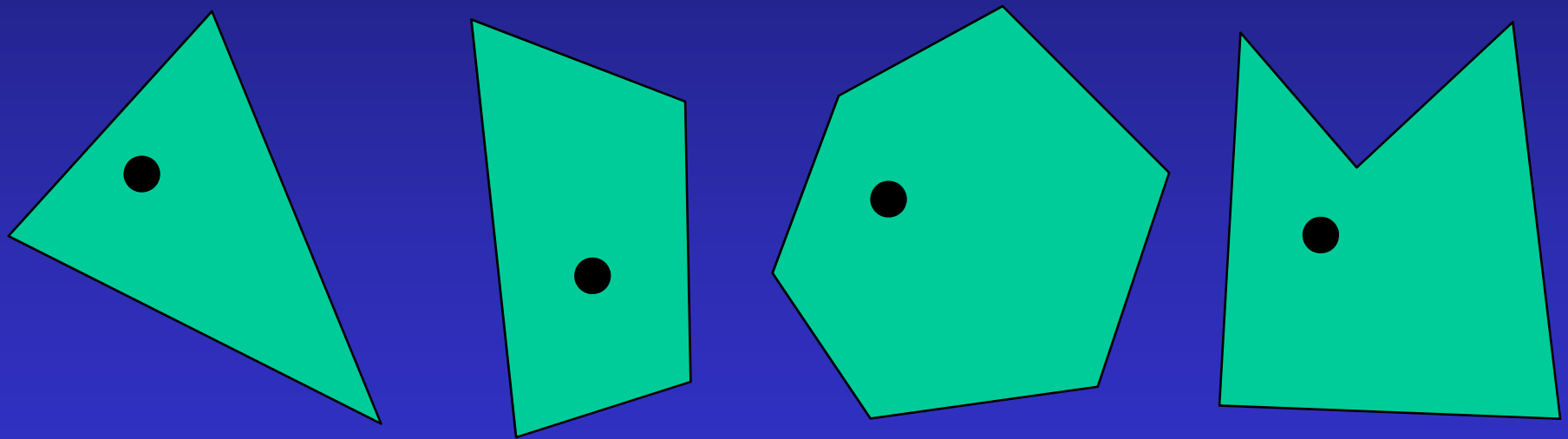
# Interpolate value(s) for point in face from values at vertices



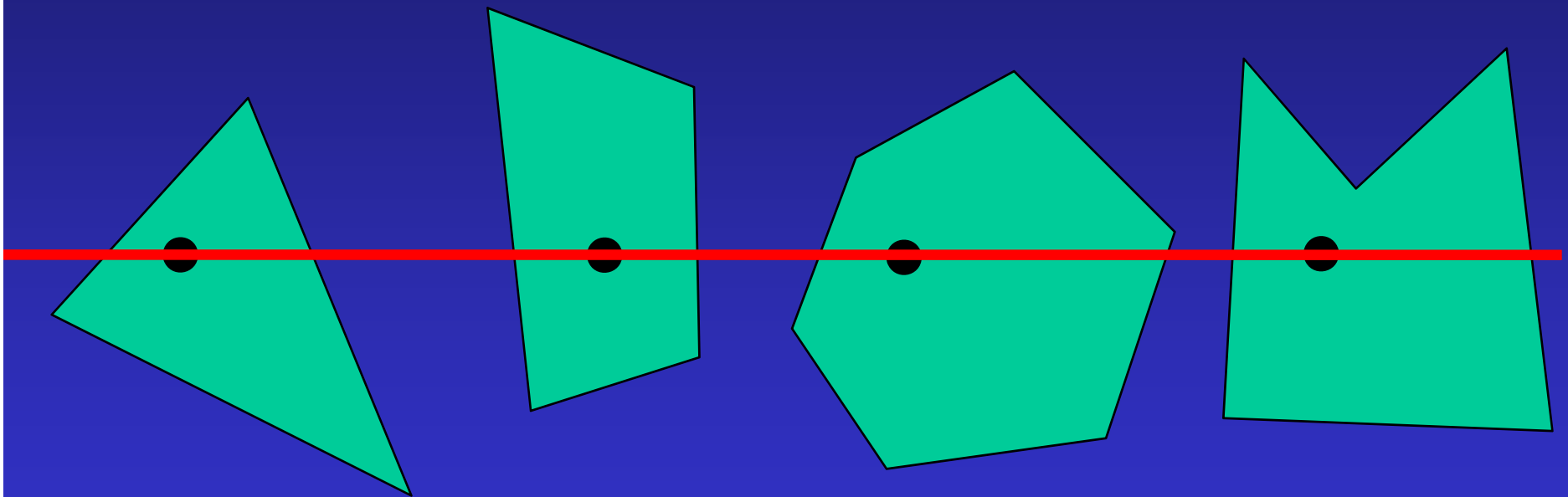
## Phong smooth shading:

- Compute normals at vertices
- Interpolate interior normal
- Compute color at point

# Interpolate value(s) for point in face from values at vertices

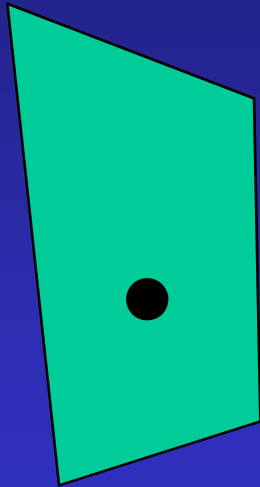


# Interpolate value(s) scanline algorithms



Interpolate down edges, across scanline

# Point sample Quadrilateral inverse binlinear map then use $u, v$ values to interpolate



$$P_{u0} = (1-u)P_{00} + uP_{10}$$

$$P_{u1} = (1-u)P_{01} + uP_{11}$$

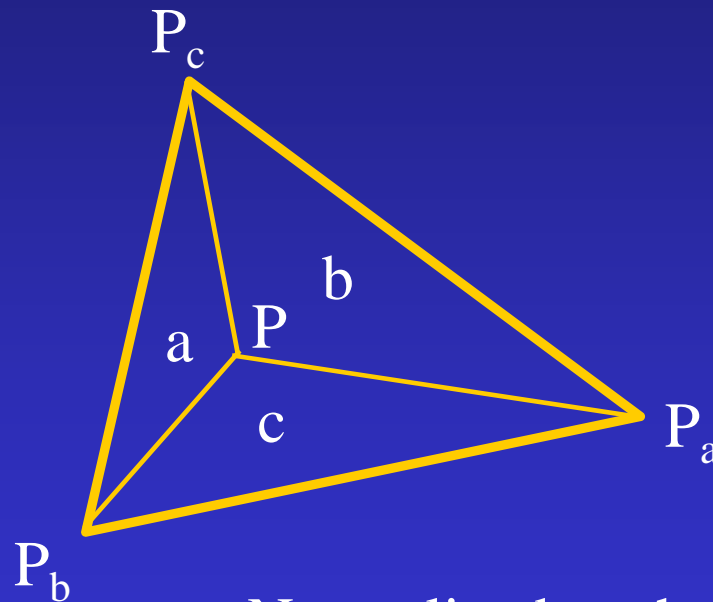
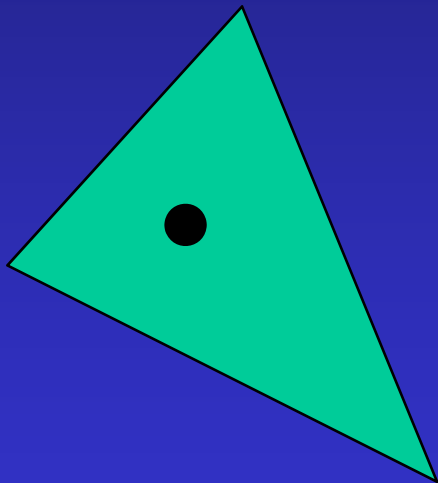
$$P_{uv} = (1-v)P_{u0} + vP_{u1}$$

$$P_{uv} = (1-v)((1-u)P_{00} + uP_{10}) + v((1-u)P_{01} + uP_{11})$$

$$P_{uv} = vu(P_{11} - P_{01} - P_{10} + P_{00}) + v(P_{01} - P_{00}) + u(P_{10} - P_{00}) + P_{00}$$

$$u = \frac{P_{uv} - P_{00} - v(P_{01} - P_{00}) - P_{00}}{v(P_{11} - P_{01} - P_{10} + P_{00}) + (P_{10} - P_{00})}$$

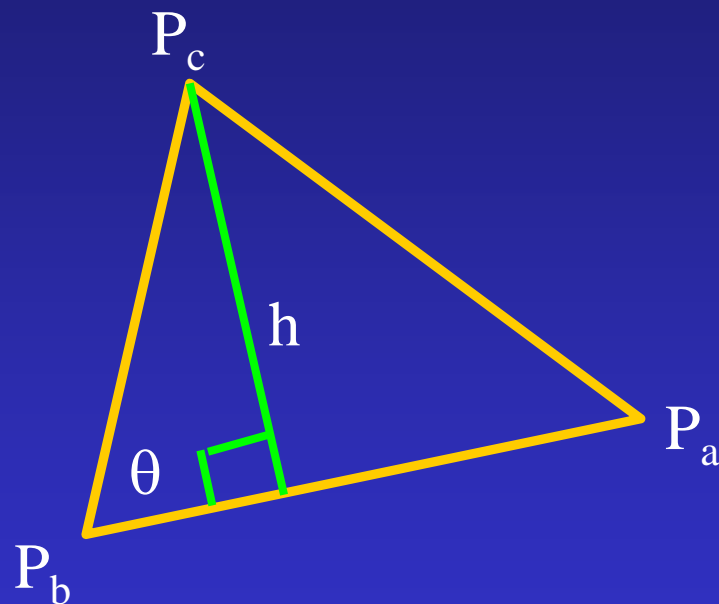
Point sample Triangle  
compute barycentric coordinates  
then use to interpolate



Normalized so that  $a+b+c=1$

$$P = aP_a + bP_b + cP_c$$

# Area of a triangle - using vector algebra



$$\text{Area} = (1/2)h|\mathbf{V}_{ab}|$$

$$h = |\mathbf{V}_{bc}| \sin(\theta)$$

$$\text{Area} = (1/2) |\mathbf{V}_{ab}| |\mathbf{V}_{bc}| \sin(\theta)$$

$$|\mathbf{V}_{ab} \times \mathbf{V}_{bc}| = |\mathbf{V}_{ab}| |\mathbf{V}_{bc}| \sin(\theta)$$

$$\text{Area} = (1/2) |\mathbf{V}_{ab} \times \mathbf{V}_{bc}|$$

# Examples of smooth shading

See links off of course web site