

CSE625 Homework 7
Due 26 Nov., 2007

1. Use the pumping lemma to show that the following languages are not CFL:
 - (a) $\{ a^i b^j c^k : i < j < k \}$.
 - (b) $\{ w \in \{a, b\}^* : n_a(x) = n_b(x)^2 \}$.
 - (c) $\{ a^n b^{3n} c^n : n \geq 0 \}$.
 - (d) $\{ a^i b^j a^i b^{i+j} : i, j \geq 0 \}$.
 - (e) $\{ w \in \{a, b, c\}^* : n_a(x) = \max\{n_b(x), n_c(x)\} \}$.

2. In each case, show that the given language is a CFL but that its complement is not. (It follows in particular that the given language is not a DCFL.)
 - (a) $\{ a^i b^j c^k : i \geq j \text{ or } i \geq k \}$
 - (b) $\{ x \in \{a, b\}^* : x \text{ is not } ww \text{ for any } w \}$